Lecture 6

The AMROC software system

Course *Block-structured Adaptive Finite Volume Methods for Shock-Induced Combustion Simulation*

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Outline

Available SAMR software

- Simplified block-based AMR
- General patch-based SAMR

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Simplified structured designs

Distributed memory parallelization fully supported if not otherwise states.

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- DAGH/Grace [Parashar and Browne, 1997]
  - Just C++ data structures but no methods
  - All grids are aligned to bases mesh coarsened by factor 2
  - http://userweb.cs.utexas.edu/users/dagh

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- SAMRAI - Structured Adaptive Mesh Refinement Application Infrastructure
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- Chombo
  - Redesign and extension of BoxLib by P. Colella et al.
  - Both multigrid and explicit algorithms demonstrated
  - Some embedded boundary support
  - https://commons.lbl.gov/display/chombo

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- Cell-based Cartesian AMR: RAGE
  - Embedded boundary method
  - Explicit and implicit algorithms
  - [Gittings et al., 2008]

AMROC

- "Adaptive Mesh Refinement in Object-oriented C++"
- $\sim 46,000$ LOC for C++ SAMR kernel, $\sim 140,000$ total C++, C, Fortran-77
- uses parallel hierarchical data structures that have evolved from DAGH

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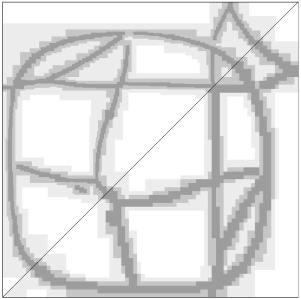
- Right: point explosion in box, 4 level, Euler computation, 7 compute nodes



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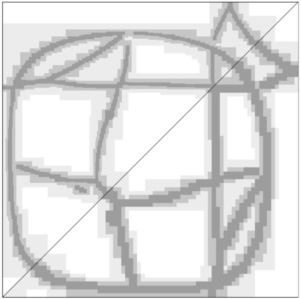
- V1.0: http://amroc.sourceforge.net



	l_{max}	Level 0	Level 1	Level 2	Level 3	Level 4
AMROC's DAGH grids/cells	1	43/22500	145/38696			
	2	42/22500	110/48708	283/83688		
	3	36/22500	78/54796	245/109476	582/165784	
	4	41/22500	88/56404	233/123756	476/220540	1017/294828
Original DAGH grids/cells	1	238/22500	125/41312			
	2	494/22500	435/48832	190/105216		
	3	695/22500	650/55088	462/133696	185/297984	
	4	875/22500	822/57296	677/149952	428/349184	196/897024

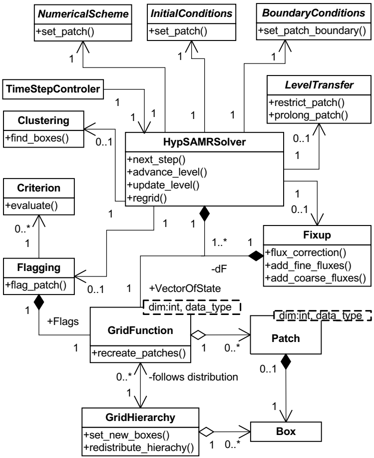
Comparison of number of cells and grids in DAGH and AMROC

The Virtual Test Facility

- Implements all described algorithms beside multigrid methods
- AMROC V2.0 plus solid mechanics solvers
- Implements explicit SAMR with different finite volume solvers
- Embedded boundary method, FSI coupling
- $\sim 430,000$ lines of code total in C++, C, Fortran-77, Fortran-90
- autoconf / automake environment with support for typical parallel high-performance system
- http://www.cacr.caltech.edu/asc
- [Deiterding et al., 2006][Deiterding et al., 2007]

UML design of AMROC

- Classical framework approach with generic main program in C++



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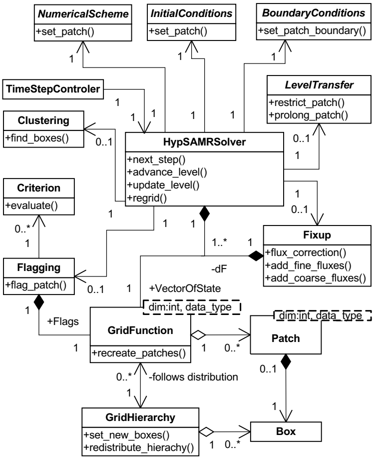

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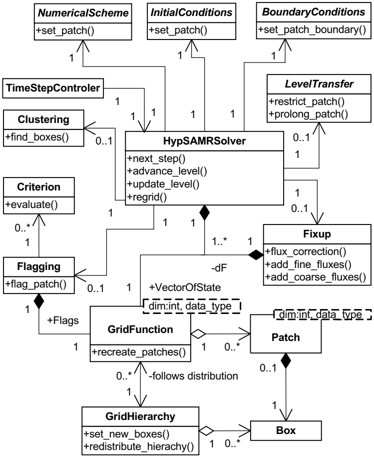

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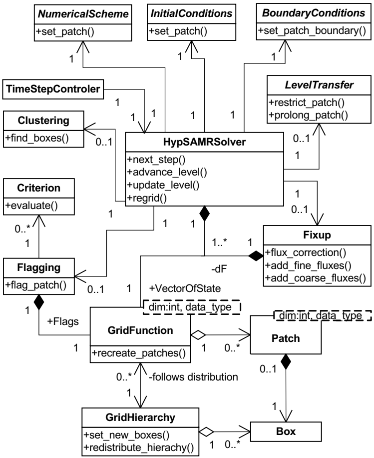

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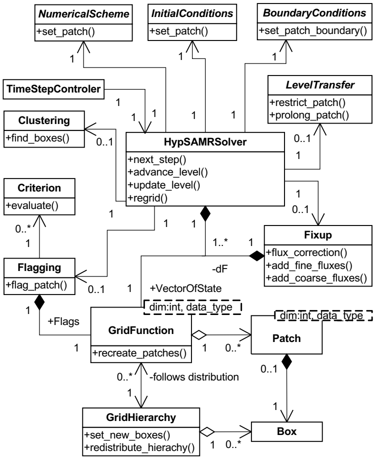

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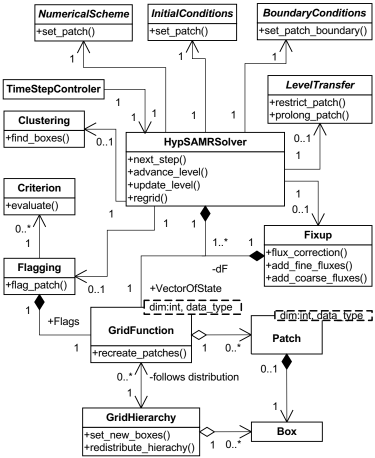
- Expert usage (algorithm modification, advanced output, etc.) in C++



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- Index coordinate system based on $\Delta x_{n,l} \cong \prod_{\kappa=l+1}^{l_{max}} r_\kappa$ to uniquely identify a cell witin the hierarchy

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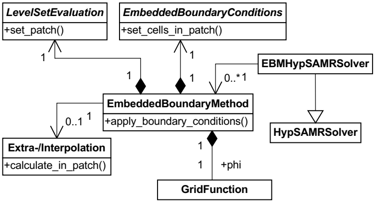
- Hierarchical parallel data structures are typically C++, routines on patches often Fortran

Embedded boundary method / FSI coupling

- Multiple independent EmbeddedBoundaryMethod objects possible
- Specialization of GFM boundary conditions, level set description in scheme-specific F77 interface classes



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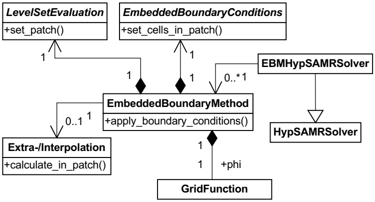

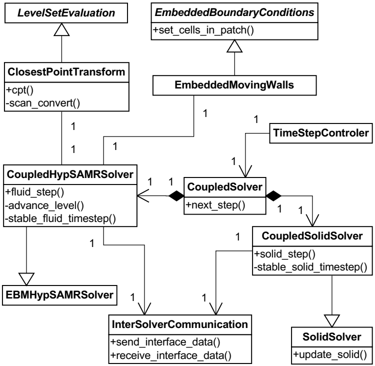

- Coupling algorithm implemented in further derived HypSAMRSolver class
- Level set evaluation always with CPT algorithm
- Parallel communication through efficient non-blocking communication module
- Time step selection for both solvers through CoupledSolver class

Parallelized construction of space-filling curve

Computation of space filling curve

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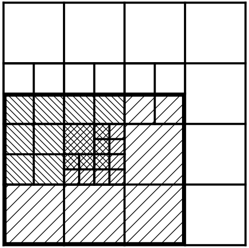

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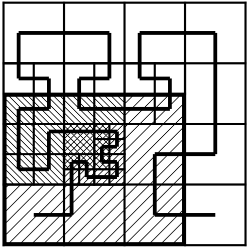

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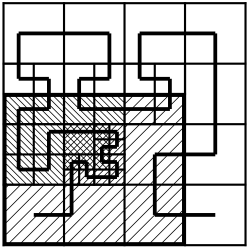

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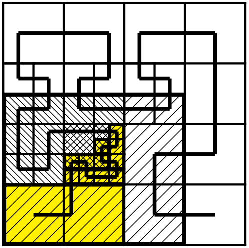

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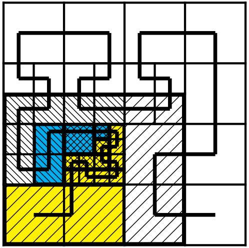

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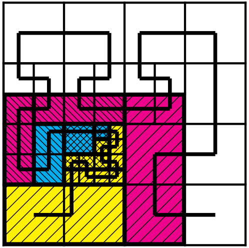

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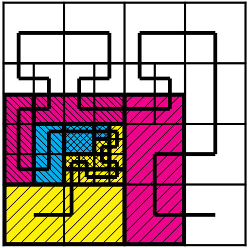

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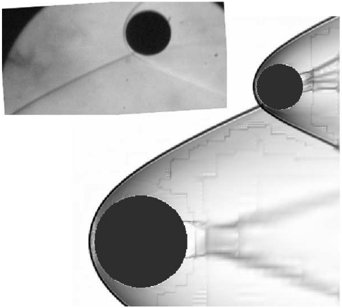
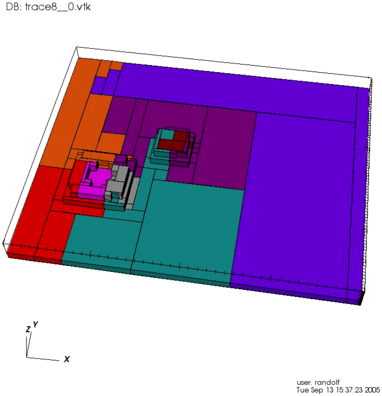
- Ensure scalability of Partition-Init by creating SFC-units strictly local
- Currently still use of `MPI_allgather()` to create globally identical input for Partition-Calc (can be a bottleneck for weak scalability)

Partitioning example





- Cylinders of spheres in supersonic flow
- Predict force on secondary body
- Right: 200x160 base mesh, 3 Levels, factors 2,2,2, 8 CPUs

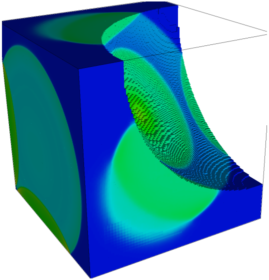
[Laurence et al., 2007]

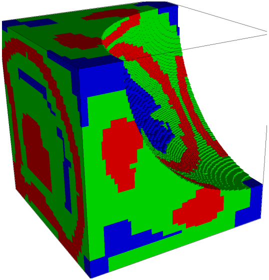
First performance assessment

- Test run on 2.2 GHz AMD Opteron quad-core cluster connected with Infiniband
- Cartesian test configuration
- Spherical blast wave, Euler equations, 3rd order WENO scheme, 3-step Runge-Kutta update
- AMR base grid 64^3, $r_{1,2} = 2$, 89 time steps on coarsest level
- With embedded boundary method: 96 time steps on coarsest level
- Redistribute in parallel every 2nd base level step
- Uniform grid $256^3 = 16.8 \cdot 10^6$ cells

Level	Grids	Cells
0	115	262,144
1	373	1,589,808
2	2282	5,907,064

Grid and cells used on 16 CPUs





Cost of SAMR and ghost-fluid method

- Flux correction is negligible
- Clustering is negligible (already local approach). For the complexities of a scalable global clustering algorithm see [Gunney et al., 2007]

CPUs	16	32	64
Time per step	32.44s	18.63s	11.87s
Uniform	59.65s	29.70s	15.15s
Integration	73.46%	64.69%	50.44%
Flux Correction	1.30%	1.49%	2.03%
Boundary Setting	13.72%	16.60%	20.44%
Regridding	10.43%	15.68%	24.25%
Clustering	0.34%	0.32%	0.26%
Output	0.29%	0.53%	0.92%
Misc.	0.46%	0.44%	0.47%

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- Costs for GFM constant around $\sim 36\%$
- Main costs: `Regrid(l)` operation and ghost cell synchronization

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Uniform	69.09s	35.94s	18.24s
Integration	59.09%	49.93%	40.20%
Flux Correction	0.82%	0.80%	1.14%
Boundary Setting	19.22%	25.58%	28.98%
Regridding	7.21%	9.15%	13.46%
Clustering	0.25%	0.23%	0.21%
GFM Find Cells	2.04%	1.73%	1.38%
GFM Interpolation	6.01%	10.39%	7.92%
GFM Overhead	0.54%	0.47%	0.37%
GFM Calculate	0.70%	0.60%	0.48%
Output	0.23%	0.52%	0.74%
Misc.	0.68%	0.62%	0.58%

AMROC scalability tests

Basic test configuration

- Spherical blast wave, Euler equations, 3D wave propagation method
- AMR base grid 32^3 with $r_{1,2} = 2, 4$. 5 time steps on coarsest level
- Uniform grid $256^3 = 16.8 \cdot 10^6$ cells, 19 time steps
- Flux correction deactivated
- No volume I/O operations
- Tests run IBM BG/P (mode VN)

AMROC scalability tests

Basic test configuration

- Spherical blast wave, Euler equations, 3D wave propagation method
- AMR base grid 32^3 with $r_{1,2} = 2, 4$. 5 time steps on coarsest level
- Uniform grid $256^3 = 16.8 \cdot 10^6$ cells, 19 time steps
- Flux correction deactivated
- No volume I/O operations
- Tests run IBM BG/P (mode VN)

Weak scalability test

- Reproduction of configuration each 64 CPUs
- On 1024 CPUs: $128 \times 64 \times 64$ base grid, $> 33,500$ Grids, $\sim 61 \cdot 10^6$ cells, uniform $1024 \times 512 \times 512 = 268 \cdot 10^6$ cells

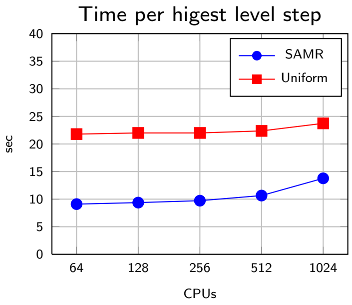
Level	Grids	Cells
0	606	32,768
1	575	135,312
2	910	3,639,040

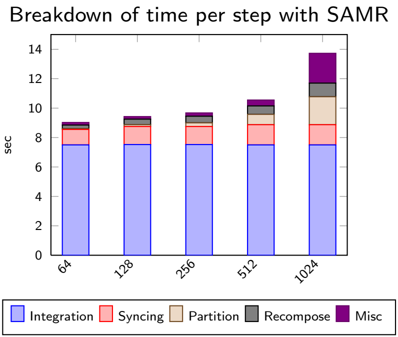
Strong scalability test

- $64 \times 32 \times 32$ base grid, uniform $512 \times 256 \times 256 = 33.6 \cdot 10^6$ cells

Level	Grids	Cells
0	1709	65,536
1	1735	271,048
2	2210	7,190,208

Weak scalability test





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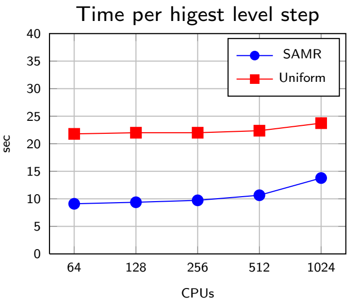
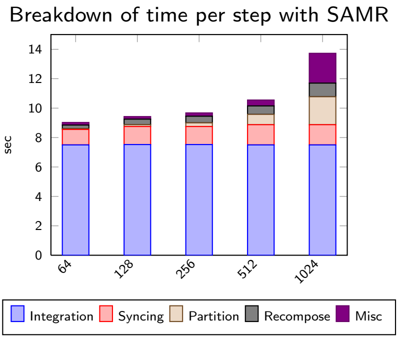
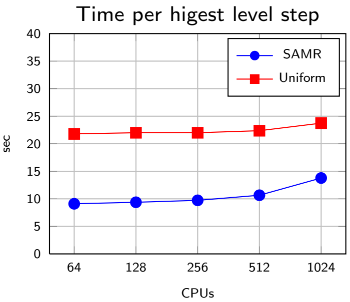
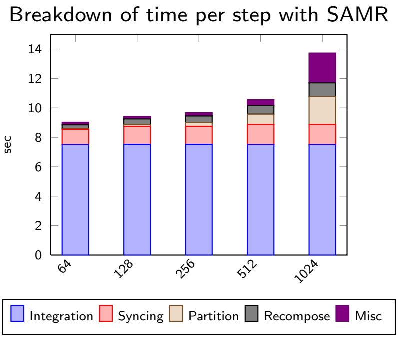




- Costs for Syncing basically constant

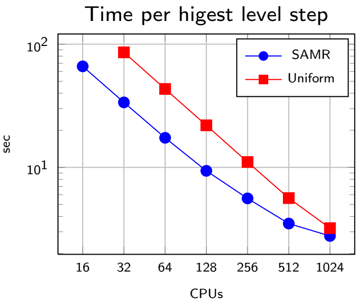
Weak scalability test

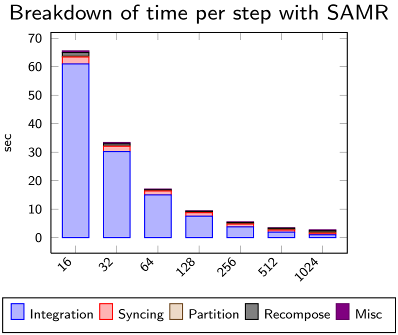




- Costs for Syncing basically constant
- Partitioning, Recompose, Misc (origin not clear) increase
- 1024 required usage of -DUAL option due to usage of global lists data structures in Partition-Calc and Recompose

Strong scalability test





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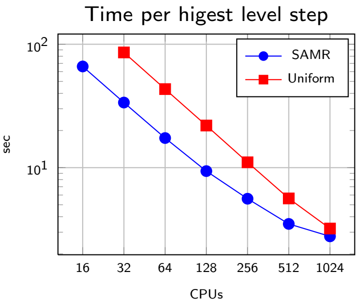
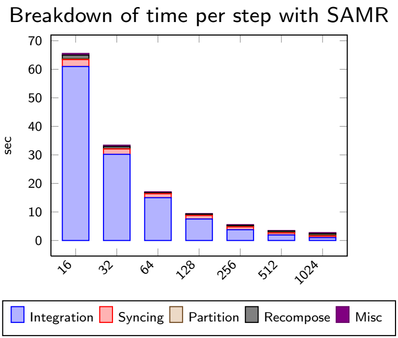
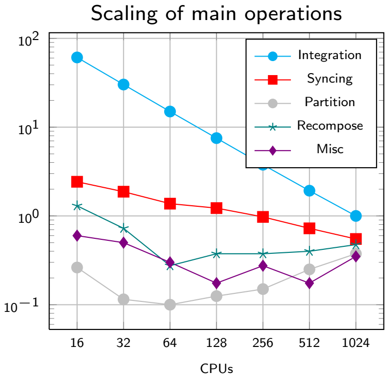
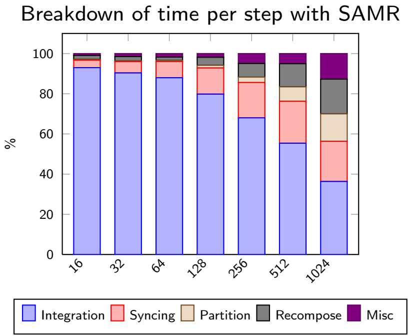




- Uniform code has basically linear scalability (explicit method)
- SAMR visibly looses efficiency for > 512 CPU, or $15,000$ finite volume cells per CPU

Strong scalability test - II





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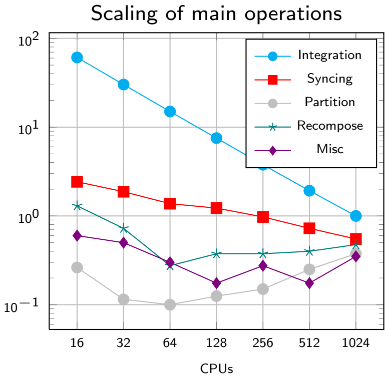
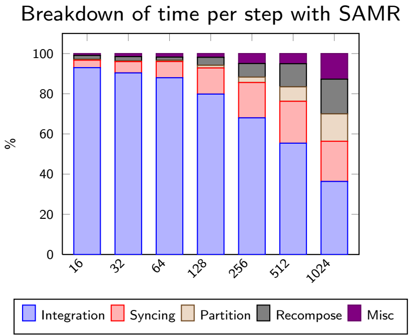
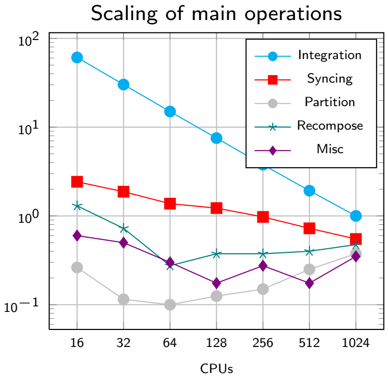
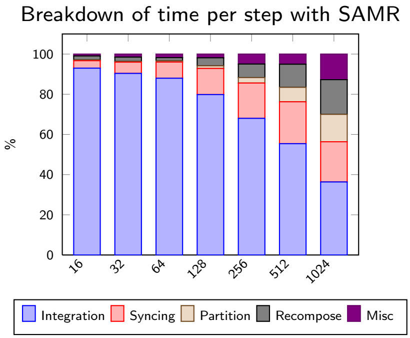




- Perfect scaling of Integration, reasonable scaling of Syncing

Strong scalability test - II

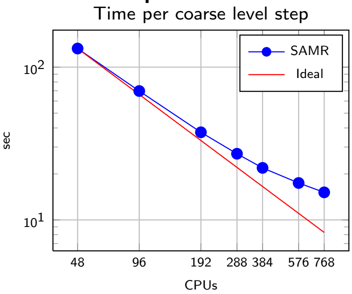




- Perfect scaling of Integration, reasonable scaling of Syncing
- Strong scalability of Partition needs to be addressed (eliminate global lists)

Strong scalability test - Train side wind computation

- Computation is restarted from disk checkpoint at $t = 0.526408\,\mathrm{s}$.
- Time for initial re-partitioning removed from benchmark.
- 200 coarse level time steps computed.
- Regridding and re-partitioning every 2nd level-0 step.
- Computation starts with 51.8M cells (l3: 10.2M, l2: 15.3M, l1: 21.5M, l0= 4.8M) vs. 19.66 billion (uniform).



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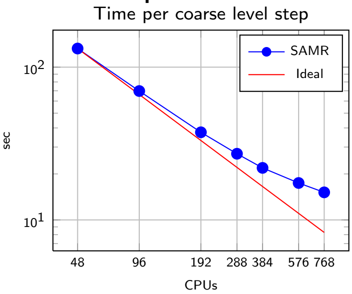

Time in % spent in main operations

Cores	48	96	192	288	384	576	768
Time per step	132.43s	69.79s	37.47s	27.12s	21.91s	17.45s	15.15s
Par. Efficiency	100.0	94.88	88.36	81.40	75.56	63.24	54.63
LBM Update	5.91	5.61	5.38	4.92	4.50	3.73	3.19
Regridding	15.44	12.02	11.38	10.92	10.02	8.94	8.24
Partitioning	4.16	2.43	1.16	1.02	1.04	1.16	1.34
Interpolation	3.76	3.53	3.33	3.05	2.83	2.37	2.06
Sync Boundaries	54.71	59.35	59.73	56.95	54.54	52.01	51.19
Sync Fixup	9.10	10.41	12.25	16.62	20.77	26.17	28.87
Level set	0.78	0.93	1.21	1.37	1.45	1.48	1.47
Interp./Extrap.	3.87	3.81	3.76	3.49	3.26	2.75	2.39
Misc	2.27	1.91	1.79	1.67	1.58	1.38	1.25

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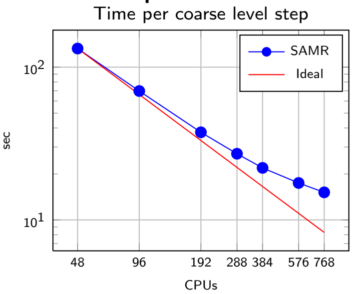
- Computation starts with 51.8M cells (l3: 10.2M, l2: 15.3M, l1: 21.5M, l0= 4.8M) vs. 19.66 billion (uniform).
- Portions for parallel communication quite considerable (4 ghost cells still used).



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